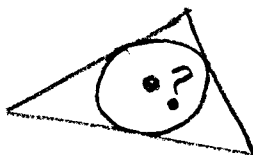


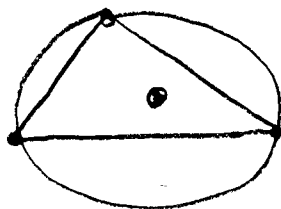
BE - Geometry I TUESDAY 2-8-11

- ① WHAT IS THE NAME OF THE CENTER OF THE circle inscribed in A triangle?



- ② How DO you FIND THIS center?

- ③ What is THE NAME OF THE CENTER OF THE circle circumscribed Around A triangle?



- ④ How DO you FIND THIS center?

- ⑤ Does $\csc^2 \theta - \cot^2 \theta = 1$?

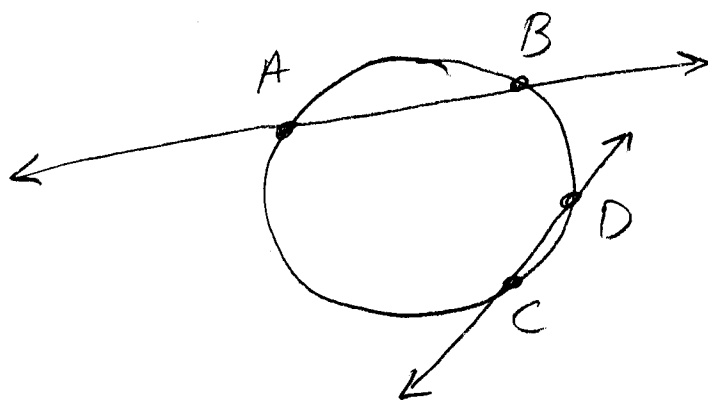
ANS

- ① INCENTER ② INTERSECTION OF Δ 'S $\angle$ bisectors.
③ CIRCUMCENTER ④ INTERSECTION OF Δ 'S perpendicular bisectors.
⑤ $\csc^2 \theta - \cot^2 \theta$

$$\begin{aligned} \frac{1}{\sin^2 \theta} - \frac{\cos^2}{\sin^2 \theta} &= \frac{1 - \cos^2 \theta}{\sin^2 \theta} \quad \left\{ \begin{array}{l} \text{Using } \sin^2 \theta + \cos^2 \theta = 1 \\ \sin^2 \theta = 1 - \cos^2 \theta \end{array} \right. \\ \Rightarrow \frac{\sin^2 \theta}{\sin^2 \theta} &= 1 \quad \checkmark \end{aligned}$$

10-6 Secants, Tangents, and Angle Measures

A line that intersects a circle in exactly 2 points is called a secant.
LATIN: "SECARE"
TO CUT

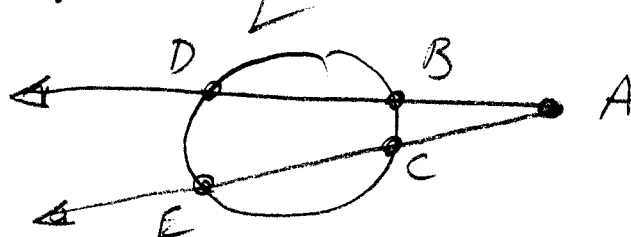


Line $\overleftrightarrow{AB}$ and $\overleftrightarrow{CD}$ are secants.

Line segment $\overline{AB}$ and $\overline{CD}$ are *chords.

*A chord is a segment of a secant.

If two secants intersect at a point, they are also RAYS



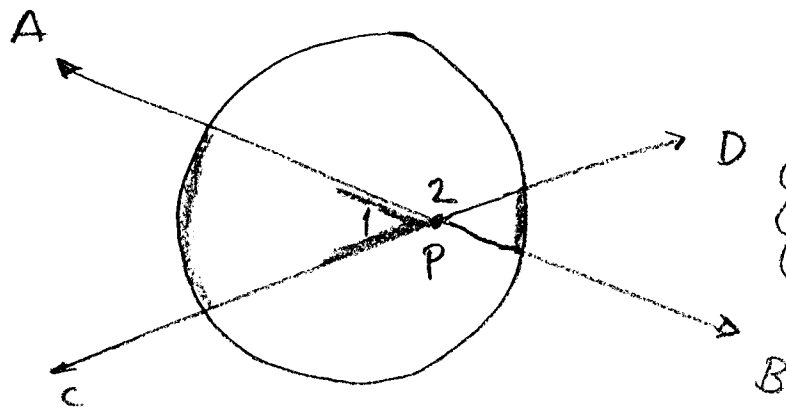
RAY $\overrightarrow{AB}$
RAY $\overrightarrow{AC}$
are secants.

THE "big" secant theory - memorize
this... Really... you need to! IDI! ✓

Theorem 10.12

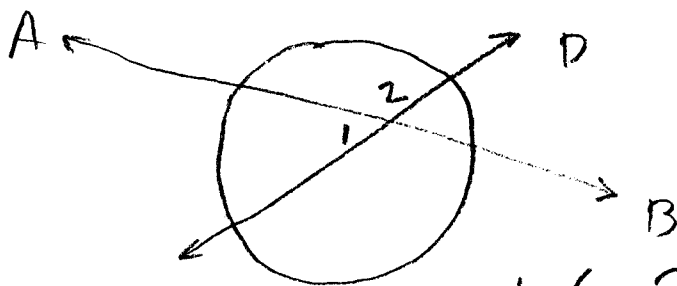
If two secants intersect in the interior of a circle, then the measure of an angle formed is $\frac{1}{2}$ the sum of the measure of the intercepted arc and the arc of its vertical angle (intercepted by)

(EX)



What happens when P moves to be on the circle?

$$m\angle 1 = \frac{1}{2} (m\widehat{AC} + m\widehat{BD})$$

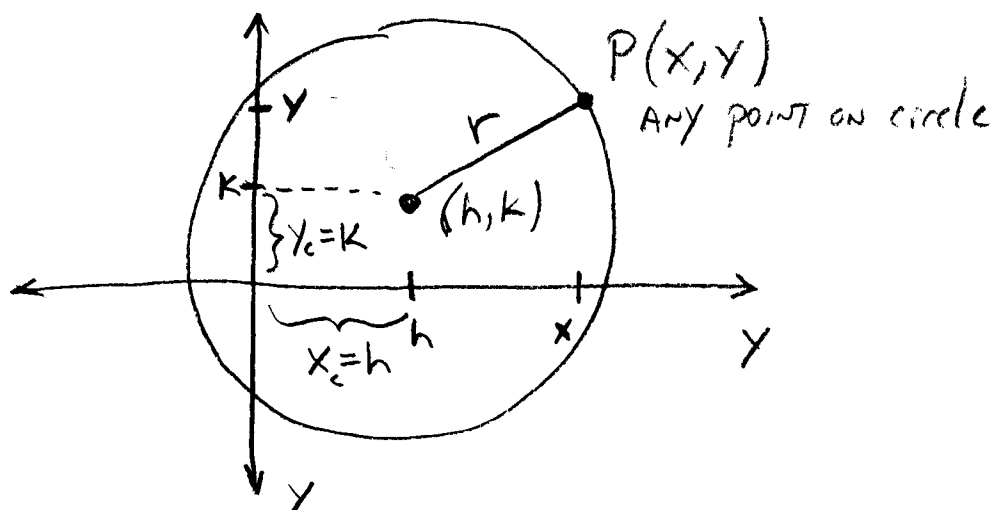


How are $\angle 1$ and $\angle 2$ related?

$$m\angle 2 = \frac{1}{2} (m\widehat{AD} + m\widehat{BC})$$

Ch.10-8 Equations of Circles

Assume (x, y) ARE THE COORDINATES OF ANY point on the below circle. The center is at (h, k) , the radius is r .



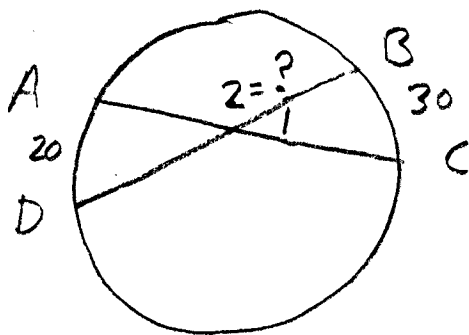
Use THE distance formula to find the distance from any $P(x, y)$ to center (h, k) which in a circle is the radius $= r$

$$\sqrt{(x-h)^2 + (y-k)^2} = r$$

or $\boxed{(x-h)^2 + (y-k)^2 = r^2}$ Equation of circle with radius r and center (h, k) .

↑
CALLED THE STANDARD FORM OF THE Eq. OF A $\odot$
I prefer "center-radius" form

Ex 1
Pg 562 Find $m\angle 2$ if $m\widehat{BC} = 30$
 $m\widehat{AD} = 20$



$$m\angle 1 = \frac{1}{2}(30 + 20) = 25^\circ$$

$$\therefore m\angle 2 = 180 - 25 = \boxed{155^\circ}$$

OR

$$\text{Since } m\widehat{BC} + m\widehat{AD} = 50^\circ$$

$$\text{The } m\widehat{AB} + m\widehat{DC} = 310^\circ$$

$$\therefore m\angle 2 \Rightarrow \frac{1}{2}(310) = \boxed{155^\circ} \checkmark$$

There are many other relationships between secants, chords, and tangents of circles (see rest of 10-6, 10-7 for ex.)

Examples

$$(x-3)^2 + (y-4)^2 = 4 \quad r=2$$

$(3,4) = \text{center}$

$$(x-5)^2 + (y-1)^2 = 5 \quad r=\sqrt{5}$$

$(5,1) = \text{center}$

$$(x-7)^2 + y^2 = 9 \quad r=3$$

$(7,0) = \text{center}$

$$x^2 + y^2 = 25 \quad r=5$$

$(0,0) = \text{center}$

$$(x+2)^2 + (y-4)^2 = 10 \quad r=\sqrt{10}$$

$(-2,4) = \text{center}$



Type into WolframAlpha:

circle $(x+2)^2 + (y-4)^2 = 10$

A center-radius form can be put into
 general form: $\boxed{x^2 + y^2 + ax + by + c = 0}$
 General Form $\odot$

$\odot$ $(x-3)^2 + (y-4)^2 = 4$

$$x^2 - 6x + 9 + y^2 - 8y + 16 = 4$$

$$\boxed{x^2 + y^2 - 6x - 8y + 21 = 0}$$

Can you go from general to center-radius form?
 Yes, by completing the square. WATCH

$$x^2 + y^2 - 6x - 8y + 21 = 0$$

Get x, y together, create holes for CTS

$$x^2 - 6x + \boxed{} + y^2 - 8y + \boxed{} = -21 + \boxed{} + \boxed{}$$

$\uparrow$
 $\frac{1}{2}b$ term squared

$$x^2 - 6x + 3^2 + y^2 - 8y + 4^2 = -21 + 9 + 16$$

$$\boxed{(x-3)^2 + (y-4)^2 = 4} \quad \checkmark$$

In other words $\Rightarrow$ the center-radius form of the eq. of a $\odot$

$$(x-h)^2 + (y-k)^2 = r^2$$

$\uparrow$
EXPAND TO
A perfect sq. trinomial

$\nwarrow$
EXPAND TO A
perfect sq. trinomial

CAN be found by "Completing the square"
for x and y since THIS is how you
create perfect square trinomials.

* Follow THE Golden Rule of Equations *

Homework: Pg 577 # 3, 4, 6, 7

Pg 578 # 10, 11, 12

Pg 564 # 12, 13, 14