

BE-PRECALCULUS | Monday 8-24-09

Mental Math Warmups:

① $8(\frac{2}{3})$ ② $\frac{1}{2}(6)$ ③ $\frac{9}{\frac{1}{3}}$

④ $\frac{-\frac{2}{5}}{\frac{1}{2}}$ ⑤ $\frac{2}{5}(12)$ ⑥ $-\frac{3}{4}(-\frac{2}{3})$

ACT - "The Real Act" $\Rightarrow$ 3 practice tests by
1 min. each 2ND Edition "THE MAKERS OF THE ACT"



⑦ If $f(x) = x^2 - 2$ then $f(x+h) = ?$

⑧ KAYA RAN $1\frac{2}{5}$ miles on Monday and $2\frac{1}{3}$ miles on Tuesday. What was the total distance, in miles, Kaya ran during those 2 days?

⑨ If $4x + 3 = 9x - 4$ then $x = ?$

$$\textcircled{7} \quad f(x) = x^2 - 2$$

$$f(x+h) = (x+h)^2 - 2$$

$$= (x+h)(x+h) - 2$$

$$= x^2 + hx + hx + h^2 - 2$$

$$= x^2 + 2hx + h^2 - 2$$

↓
OR $2xh$

$$\textcircled{8} \quad 1\frac{2}{5} + 2\frac{1}{3} \Rightarrow \frac{2}{5} + \frac{1}{3}$$

$$\frac{6}{15} + \frac{5}{15} = \frac{11}{15}$$

$$= 3\frac{11}{15} \text{ miles}$$

$$\textcircled{9} \quad \begin{array}{r} 4x + 3 = 9x - 11 \\ -4x + 4 \quad -4x + 4 \end{array}$$

$$\frac{7}{5} = \frac{5x}{5}$$

$$\boxed{\frac{7}{5} = x}$$

PRECALCULUS

- The importance of doing a good job on homework

	<u>HW 1</u>	<u>Quiz 1</u> *	* 4-Answer multiple choice $\Rightarrow$ 0% ~ 25%
	0%	25%	
	0%	33%	
Lowest	30%	42%	
to			
HW	41%	75%	
	50%	67%	
	<u>59%</u>	<u>75%</u>	
Highest	111%	100%	
to	107%	92%	
HW	96%	100%	
	95%	92%	
	95%	100%	
	94%	75%	

- Small, 12 question quiz over Ch 1-2
- The longer, harder topics widen this gap.
- No precalc student can claim Ch 1-2 is "out of reach"

A little review:

"like" terms $\Rightarrow$ 1. SAME variable
2. variables have SAME exponent

"COMBINE" Like terms $\Rightarrow +$ or $-$

Ex) $\underline{2x} + \underset{\checkmark}{3y} \text{ } \textcircled{-z} \text{ } \boxed{+4} + \underline{5xy} + \underline{3x} - \underline{2xy} + 4x^2$

$$\begin{array}{ccccccc} 5x & + & 3y & - & z & + & 4 & + & 3xy & + & 4x^2 \\ \uparrow & & \uparrow & & \uparrow & & \uparrow & & \uparrow & & \uparrow \\ \text{degree 1} & & \text{degree 1} & & \text{degree 1} & & & & \text{degree 2} & & \text{degree 2} \end{array}$$

The degree of a single term is the sum
(monomial)
of the exponents of all its variables

$$4x^2 + 3xy + 5x + 3y - z + 4$$

Sign Rules: $+, -$ SSA, KSS "same sign add, keep same sign"

Ex) $2 + 6 = 8$
 $-2 - 6 = -8$

DSD, BOW "different signs take their difference, biggest one wins"

Ex) $-2 + 6 = 4$
 $2 - 6 = -4$

SPECIAL "taking away a $-$ is a $+$ "

Ex) $-2 - (-6) = -2 + 6 = 4$

$\cdot, \div$ SPDN "same signs $+$, diff. signs $-$ "

Ex) $-2(-2) = 4$ $\frac{-2}{-2} = 1$
 $-2(2) = -4$

F.R.

$+, -$ CD

$\cdot$ $\frac{a+b}{b-b}$

$\div$ FEM

If you have an equation in 2 variables,
say x and y , and the x terms and y terms
are only to the first power (x' , y')
then you will have a linear equation.

The graph of the equation is a line.

You can always combine all the x' terms,
 y' terms, and numbers. The Standard Form

of a LE is $Ax + By = C$

$\uparrow$ ALL the x' terms combined
 $\uparrow$ ALL the y' terms combined
 $\uparrow$ ALL THE NUMBERS

CONVENTIONS $A > 0$

A , B , and C are NOT fractions

ⓧ $2x + 3y = 7$

ⓧ $\frac{1}{3}x + \frac{2}{5}y = 2 \Rightarrow 5x + 6y = 30 \Rightarrow SF$

ⓧ $-5x + y = 6 \Rightarrow 5x - y = -6 \Rightarrow CAS$
 CHANGE ALL SIGNS

If instead of combining all terms, you solved to get y "by itself", you will get this form:

$$y = mx + b$$

↑
SLOPE

↓
 $\frac{\text{rise}}{\text{run}} = m$

↑

$(0, b)$

IS THE POINT ON THE LINE WHERE IT CROSSES THE y -AXIS, b is called the y -intercept

SLOPE-INTERCEPT FORM
(OF A LINEAR EQUATION)

⑧ $y = 3x - 2$

↑
 $m = \oplus \frac{3}{1}$

↑
 $(0, -2)$

CROSSES y -AXIS

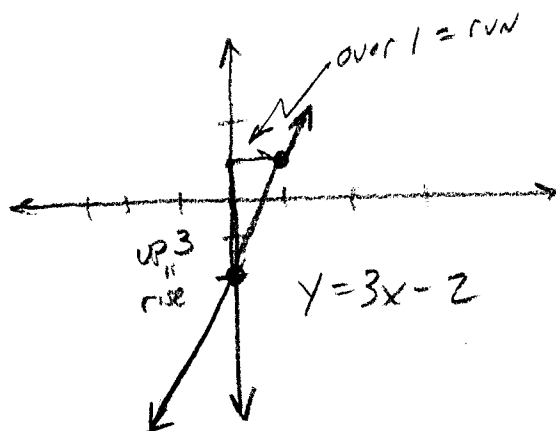
$y = f(x) = mx + b$

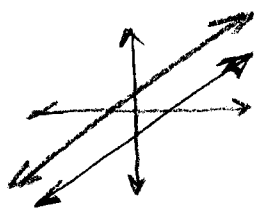
↑
'function' form

Graph
TIP

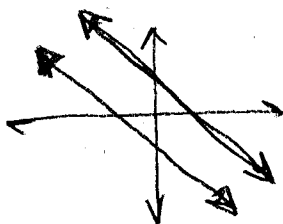


begin at b
move by slope





+m
POSITIVE SLOPES



-m
NEGATIVE SLOPES

horizontal
 $m=0$

$$\frac{\text{RISE}}{\text{RUN}} = \frac{0}{\text{RUN}}$$

4.
VERTICAL
 $m = \text{UNDEFINED}$
 $\frac{\text{RISE}}{\text{RUN}} = \frac{\text{RISE}}{0}$
↑
UNDEFINED

X-intercept $\Rightarrow (x, 0)$

Y-intercept $\Rightarrow (0, y)$

EX 1 Pg 20

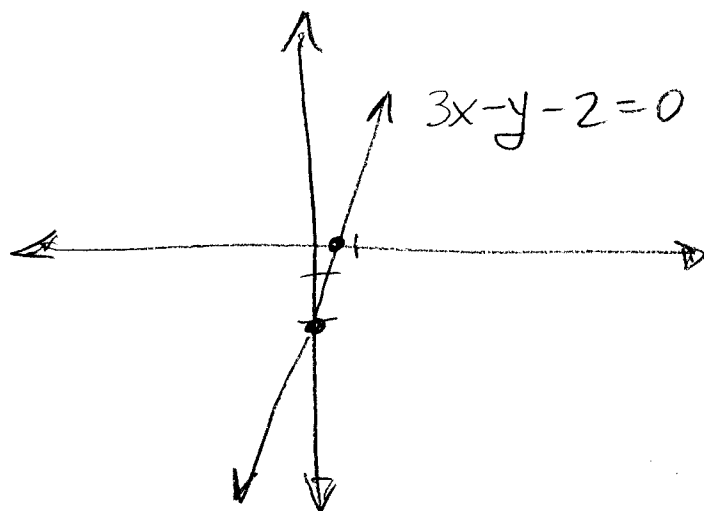
GRAPH $3x - y - 2 = 0$ USING MOI
METHOD OF
INTERCEPTS

$$y_{\text{INT}} \Rightarrow x=0 \therefore 3(0) - y = 2$$

$$y = -2 \Rightarrow (0, -2)$$

$$x_{\text{INT}} \Rightarrow y=0 \therefore 3x - 0 = 2$$

$$x = \frac{2}{3} \Rightarrow \left(\frac{2}{3}, 0\right)$$



LOOK AT SI Form

$$3x - y = 2$$

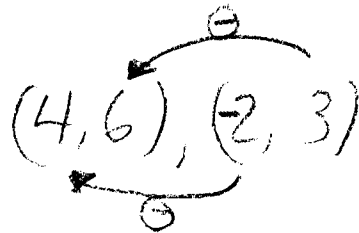
$$-y = -3x + 2$$

$$\boxed{y = 3x - 2}$$

If you know the coordinates of any 2 points on the line,

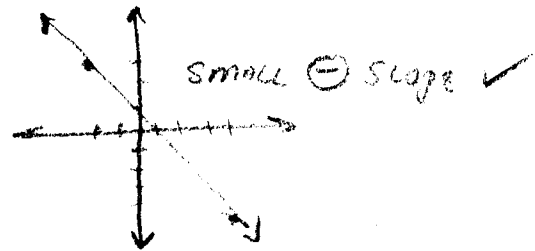
$$m = \frac{\text{rise}}{\text{run}} = \frac{\text{change in } Y}{\text{change in } X} = \frac{Y_2 - Y_1}{X_2 - X_1}$$

EX Find m through $(4, 6), (-2, 3)$



$$m = \frac{3 - 6}{-2 - 4} = \frac{-3}{-6} = \frac{1}{2}$$

CK



The X -intercepts $\Rightarrow y = 0$ are also called the zeros of the function.

If $y = f(x) = mx + b$

If $0 = mx + b$

$$\frac{-b}{m} = \frac{mx}{m}$$

$$\therefore x = \frac{-b}{m} = \text{Zero of the function}$$

(X-intercept)
↓
($-\frac{b}{m}, 0$)

Homework: Read Ch 1-3
Graphing Linear Equation Pg. 23 & 24 #11-17, 24-26